

## Year 13 Pure

### Teacher A

#### Algebraic methods and proof

- Know and apply the various types of proof (proof by contradiction, exhaustive proof etc)
- Add and subtract algebraic fractions
- Multiply and divide algebraic fractions
- Application of the factor theorem
- Factorising polynomial completely
- Partial proper fractions
- Partial improper fractions
- Algebraic division

#### Series and sequences

- Sequence of numbers (finite and infinite)
- Difference between sequence and series
- Convergent and divergent sequence
- Difference between arithmetic and geometric sequence
- Nth term and sum of terms of AP
- Nth term and sum of terms of GP
- Sum of GP to infinity and conditions
- Solve problems involving AP and GP
- The use of the sigma notation
- Difference between increasing, decreasing and periodic sequence
- Application of recurrence and iteration to solve sequence problems

### Teacher B

#### Functions and modelling

- Modulus function and its graphs
- Solve equations and inequalities involving modulus functions
- Domain and range of functions
- One-to-one and many-to-one functions
- Composite functions
- Inverse of a function and sketch the graphs
- Conditions for inverse function to exist
- Transformation of functions
- Composite transformation of functions and describe their effect geometrically
- Solve problems involving modulus and transformation

#### Binomial Expansion

- Know that the year 12 formula for binomial expansion fails when the power is not an whole number
- Binomial expansion for negative and fractional powers
- Binomial expansion and problem solving
- Partial fraction and binomial expansion
- Percentage error

<p>Radian</p> <ul style="list-style-type: none"> <li>- Understand the definition of radian</li> <li>- Convert between radian and degree</li> <li>- Exact value of sin, cos and tan in radian</li> <li>- Derive and use the formula for arc length and area of sector</li> <li>- Solve trigonometric equations with a given interval in radian</li> <li>- Application of the two trig identities taught in year 12 to solve trig equations</li> <li>- Small angle approximation for sin, cos and tan.</li> </ul>	<p>Parametric equations</p> <ul style="list-style-type: none"> <li>- Understand the difference between cartesian and parametric systems of expressing coordinates</li> <li>- Convert between parametric and cartesian coordinates</li> <li>- Plot and sketch curves in parametric form</li> <li>- Solve coordinate geometry problems using parametric equations</li> <li>- Recognise some standard curves in parametric and use them to solve problems</li> </ul>
<p>Trigonometric functions</p> <ul style="list-style-type: none"> <li>- Understand secant, cosecant and cotangent and their graphs</li> <li>- Simplify expressions and solve equations involving sec, cosec and cot</li> <li>- Derive and apply identities for sec, cosec and cot and apply them to solve trig equations</li> <li>- Work with the inverse trig functions and sketch their graphs</li> <li>- Trigonometric proofs</li> </ul>	<p>Differentiation</p> <ul style="list-style-type: none"> <li>- Find the derivative of <math>\sin x</math> and <math>\cos x</math> from first principle</li> <li>- Differentiate <math>e^{kx}</math> and <math>\ln x</math> functions and sketch their graphs</li> <li>- Equation of tangents and normal to <math>y = e^{kx}</math> and <math>y = \ln x</math> functions</li> <li>- Know and apply the chain rule</li> <li>- Know and apply the product rule</li> <li>- Know and apply the quotient rule</li> <li>- Apply differentiation rules to trig functions</li> <li>- Parametric differentiation</li> <li>- Gradient at a given point from a parametric equations</li> <li>- Equation of tangent and normal to parametric functions</li> <li>- Implicit differentiation involving two variables</li> <li>- Gradient of a curve using implicit differentiation</li> <li>- Stationary point and implicit differentiation</li> <li>- Nature of stationary point and rate of change</li> </ul>

	<ul style="list-style-type: none"> <li>- Find the value of an exponential function after a given time</li> <li>- Equation of exponential growth problems</li> </ul>
<b>Mock Exam (Everything including year 12 work except: Integration, vectors and numerical methods)</b>	
<b>Trigonometry and modelling</b> <ul style="list-style-type: none"> <li>- Use the compound angle identities to rearrange expressions</li> <li>- Use the compound angle identities to rearrange and solve equations</li> <li>- Proof geometrically the three compound angle formulae</li> <li>- Prove other identities using the compound angle identities</li> <li>- Double angle formula and other identities</li> <li>- Triple angle formula and other identities</li> <li>- Express <math>a \cos \theta + b \sin \theta</math> as a single sine or cosine function</li> <li>- solve equations of the form <math>a \cos \theta + b \sin \theta = c</math> in a given interval</li> <li>- Modell and solve trig functions to solve problems in context, including those involving vectors, kinematics and forces</li> </ul>	<b>Integration</b> <ul style="list-style-type: none"> <li>- Integration by inspection using the reverse of differentiation</li> <li>- Know that integral of <math>1/x = \ln x</math> and integral of <math>e^x = e^x</math></li> <li>- Integration by substitution</li> <li>- Integration by part</li> <li>- Integration of trigonometric expressions</li> <li>- recognise integrals of the form <math>\int \frac{f'(x)}{f(x)} dx = \ln  f(x)  + c</math>;</li> <li>- Use trigonometric identities to manipulate and simplify expressions to a form which can be integrated directly.</li> <li>- Integrating rational expressions by using partial fractions with linear denominators</li> <li>- Simplify integral of rational functions using the laws of logarithm</li> <li>- Area under a curve or between two given points</li> <li>- Use the trapezium rule to estimate area under a curve and determine if it overstate or understate the actual area.</li> <li>- Write a differential equation from worded problems</li> <li>- Solve differential equation</li> <li>- Find particular solutions of differential equations</li> </ul>
<b>Numeric method</b> <ul style="list-style-type: none"> <li>- Locate roots by considering change in sign</li> </ul>	<ul style="list-style-type: none"> <li>•</li> </ul>

<ul style="list-style-type: none"> <li>- Use numerical methods to solve solutions of equations</li> <li>- Iteration</li> <li>- Staircase and cobweb diagram</li> <li>- Convergence and iteration</li> <li>- Solve equations approximately using Newton-Raphson method</li> <li>- Understand that the Newton-Raphson method works in geometrical terms</li> <li>- Problem solving and numerical method</li> </ul>	
<p>Vectors</p> <ul style="list-style-type: none"> <li>- Vectors in three dimensions</li> <li>- Magnitude of 3D vectors</li> <li>- Unit vector and its application</li> <li>- Add and subtract 3D vectors</li> <li>- Scalar multiplication of 3D vectors</li> <li>- Position vectors and distance between two points</li> <li>- Vectors and problem solving</li> </ul>	<ul style="list-style-type: none"> <li>•</li> </ul>

## Year 13 Applied

### Teacher A- Statistics

### Teacher B- Mechanics

#### Regression, correlation and Hypothesis testing

- Change variables of regression line by using logarithms
- Estimate values from regression line
- Correlation coefficient interpretation
- Product moment correlation coefficient and its interpretation
- Hypothesis testing of PMCC

#### Forces at any angle (part 1)

- Language of forces
- Identify all forces acting on a particle and represent them diagrammatically
- Finding the resultant force (magnitude and direction)
- Resultant of several concurrent forces
- Resolve forces into components and select suitable resolutions

#### Probability

- Use probability formulae and notations
- Use probability tree diagrams
- Use Venn diagrams and its components
- Use two-way table
- Use the conditional probability formula  

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$
- Model with probability
- Critique assumptions made and the likely effect of more realistic assumptions

#### Further kinematics (part 1)

- Use of constant acceleration formulae
- Position vectors, velocities, acceleration, and displacement in vector form
- Language of kinematics in 2D
- Use velocity triangles and problem solving
- SUVAT constant acceleration in 2D
- Apply the equations of motion to **i, j** vector problems
- Use  $\mathbf{v} = \mathbf{u} + \mathbf{at}$ ,  $\mathbf{r} = \mathbf{ut} + \frac{1}{2}\mathbf{at}^2$  etc. with vectors given in **i, j** or column vector form.

#### Normal distribution

- Properties of normal distributions
- Calculate probabilities from normal distributions
- know the position of the points of inflection of a Normal distribution.
- Mean and variance of a normal distribution
- Understand and apply continuity corrections
- Use the Normal distribution as an approximation to the binomial distribution.
- Statistical hypothesis test for the mean of normal distributions

#### Application of kinematics – Projectile

- Understand factors affecting projectile
- Find time of flight of a projectile
- Find range and maximum height of a projectile
- derive formulae to find the greatest height, the time of flight and the horizontal range (for a full trajectory)
- Modify projectile equations to take account of the height of release;
- Derive and use the equation of the path.

<ul style="list-style-type: none"> <li>- Interpret results of the hypothesis testing in context</li> </ul>	
	<p>Forces at any angle (part 2)</p> <ul style="list-style-type: none"> <li>- Understand that a rough plane creates frictional force which act against direction of motion</li> <li>- Roughness' of two surfaces is represented a coefficient of friction represented by <math>\mu</math>;</li> <li>- Know that <math>0 \leq \mu</math> but that there is no theoretical upper limit for <math>\mu</math> although for most surfaces it tends to be less than 1 and that a 'smooth' surface has a value of <math>\mu = 0</math>;</li> <li>- Draw force diagrams involving rough surfaces which include the frictional force</li> <li>- Limiting equilibrium formula <math>F \leq \mu R</math>.</li> </ul>
	<p>Application of forces (part 1)</p> <ul style="list-style-type: none"> <li>- Equilibrium under a set of concurrent forces (resultant = 0)</li> <li>- Vectors representing forces in equilibrium form a closed polygon;</li> <li>- Solve problems involving equilibrium of a particle under coplanar forces, including particles on inclined planes and 2D vectors;</li> <li>- Understand and apply Newton's second law of motion</li> <li>- <math>F = ma</math> for 1 dimensional motion</li> <li>- Formulate and solve equations of motion for a particle in 2D motion where the resultant = <math>ma</math></li> <li>- Formulate and solve equations of motion for connected particles, where one of the parts could be inclined and/or on a rough plane.</li> </ul>
	<p>Further kinematics (part 2)</p> <ul style="list-style-type: none"> <li>- Extend techniques for 1D to 2D by using vectors of equations for variable forces/acceleration</li> </ul>

	<ul style="list-style-type: none"><li>- Know and apply the language and notation for Kinematics for variable motions in 2D</li></ul>
	<p>Moment: forces' turning effect</p> <ul style="list-style-type: none"><li>- Know that moment = perpendicular force times distance</li><li>- Draw mathematical model to represent horizontal rod problems</li><li>- Conditions for equilibrium and apply them</li><li>- Solve problems when a beam is at the point of tilting</li></ul>
	<p>Applications of forces (part 2)</p> <ul style="list-style-type: none"><li>- Solve statics problems for a system of forces which are not concurrent (ladder) and apply the principles of moments for forces at any angle</li></ul>